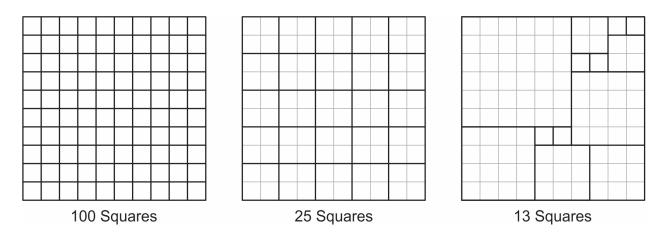
# MJ4MF - ONE-HUNDRED PROBLEMS

#### **Covered with Squares**

As shown below, a square grid with 100 smaller squares can be covered by 100 squares (each measuring  $1 \times 1$ ), by 25 squares (each measuring  $2 \times 2$ ), or by 13 squares (one  $6 \times 6$ , two  $4 \times 4$ , two  $3 \times 3$ , two  $2 \times 2$ , and six  $1 \times 1$ ).



Find all values of *n* for which it's impossible to cover a  $10 \times 10$  grid with *n* squares of integer side length.



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### It's Gettin' Kinda Heavy

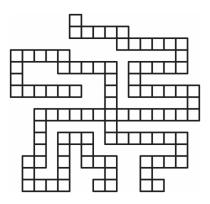
Which weighs more: \$100 worth of quarters, or \$100 worth of dimes?

### Why, Certainly

For what value of *n* can you be certain that *n* consecutive positive integers have a product that is divisible by 100?

#### Around the Square

The figure below consists of 100 unit squares, and adjacent squares share a side. What is the perimeter of the figure?



## **Magic Rectangles**

A magic rectangle is an  $m \times n$  array of the positive integers from 1 to  $m \times n$  such that the numbers in each row have a constant sum and the numbers in each column have a constant sum (although the row sum need not equal the column sum). Shown below is a  $3 \times 5$  magic rectangle with the integers 1 to 15.

6	7	8	9	10
13	3	1	11	12
5	14	15	4	2

How many magic rectangles can be made using the integers 1 to 100?

These problems appear in **One-Hundred Problems Involving the Number 100**, available from NCTM. If you're interested in the other 95%, click the link below: https://www.nctm.org/Store/Products/One-Hundred-Problems-Involving-the-Number-100/

